

Weaving Parallel Threads

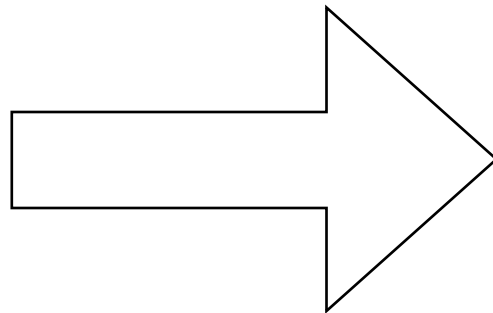
Searching for Useful Parallelism in Functional Programs

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Vision

automated
parallelisation

program written
without reference
to parallelism



transformed program
exploits parallelism
of target hardware

Desirable Properties

safe

transformed program
is functionally correct

worthwhile

transformed program
is faster

Our Approach

safe

transformed program
is functionally correct

worthwhile

transformed program
is faster

static analysis

what **can** be parallelised?

metaheuristic search

what **should** be parallelised?

Context: Functional Programs

Purity

```
second (x:y:xs) = y
```

```
myList = [3,8,7,4]
```

```
> second myList  
8
```

Lazy Evaluation

```
errList = [head [], 12, 3]
```

```
> second errList  
12
```

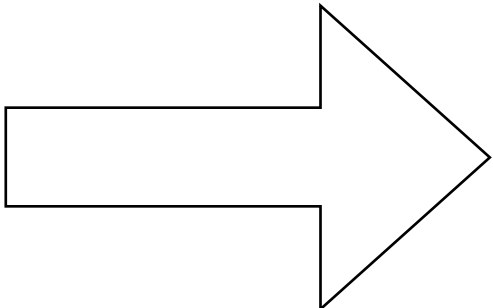
```
infList x = x:(infList (x+1))
```

```
> second infList 3  
4
```

par primitive

par a b

returns result of **b** while evaluating **a** in a new thread

f x  par x (f x)

speculatively evaluate argument in parallel

Safe Parallelisation: Static Analysis

Strictness Analysis

```
errList = [head [], 12, 3]
```

```
> par (force errList) (f errList)  
EXCEPTION: ...
```

```
infList = x:(infList (x+1))
```

```
> par (force infList) (f infList)
```

par-sites

```
eulerLL_15 = let
  v_15 = filterDefrelPrime v_15 (fromto_D2 1 v_15)
  (fix eulerLL_0 v_164) (length v_164));

eulerLL_1 v_16 v_17 = case v_17
of {
  <0> v_168 v_169 ->
    seq v_169 Pack{0,0};
  <1> -> Pack{0,0}
};

eulerLL_0 v_18 = eulerLL_1 v_18;

ifte v_19 v_20 v_21 = case v_19
of {
  <1> -> v_20;
  <0> -> v_21
};

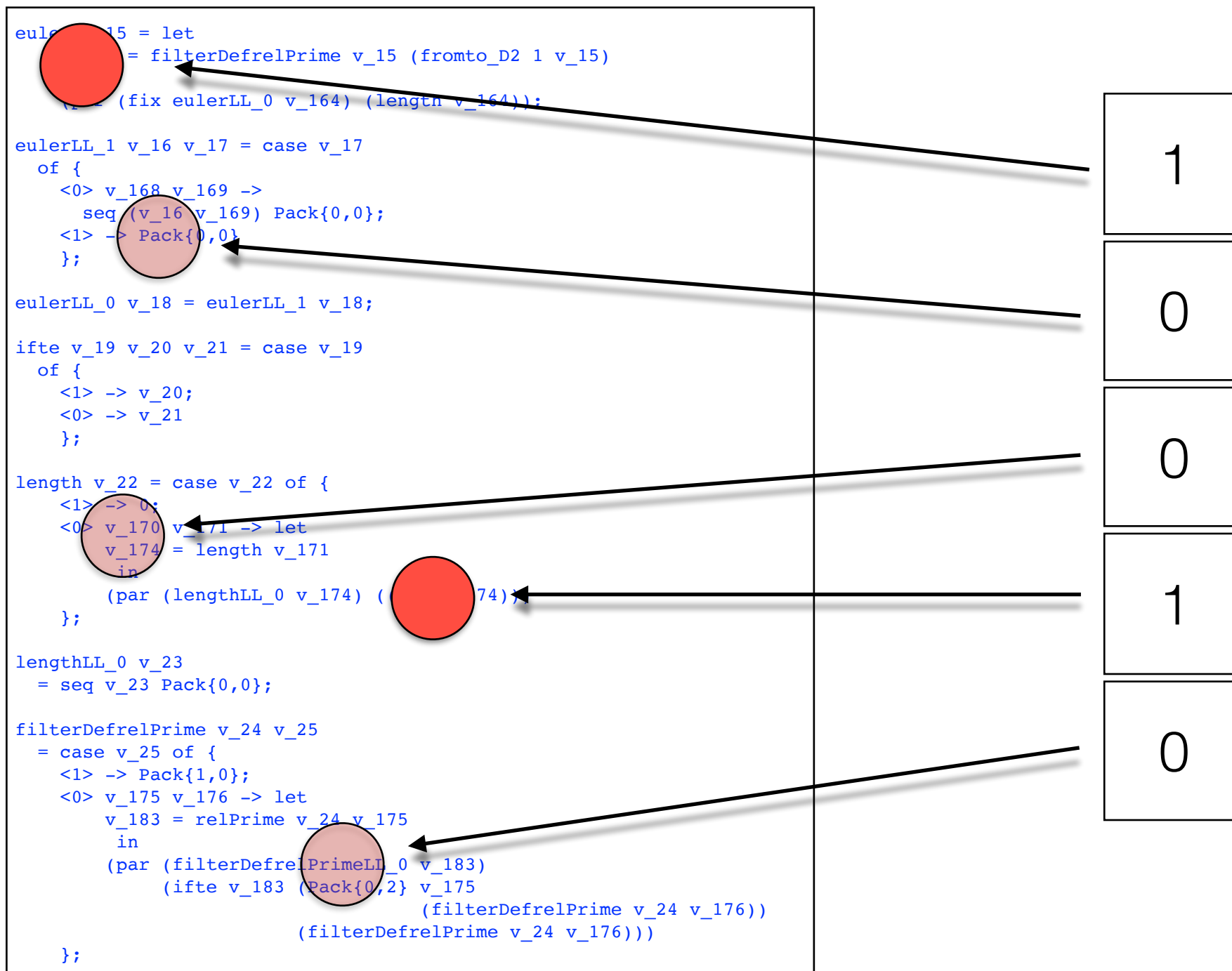
length v_22 = case v_22 of {
  <1> -> v_22;
  <0> v_171 -> let
    v_171 = length v_171
  in
    (par (lengthLL_0 v_174) (lengthLL_0 v_174));
};

lengthLL_0 v_23
= seq v_23 Pack{0,0};

filterDefrelPrime v_24 v_25
= case v_25 of {
  <1> -> Pack{1,0};
  <0> v_175 v_176 -> let
    v_183 = relPrime v_24 v_175
  in
    (par (filterDefrelPrime v_183 v_183)
      (ifte v_183 (filterDefrelPrime v_175 v_175)
        (filterDefrelPrime v_24 v_176)))
    (filterDefrelPrime v_24 v_176));
};
```

Worthwhile Parallelisation: Metaheuristic Search

Representation



Fitness

Target Environment

```
eulerLL_0 v_15 = let
  eulerLL_0 v_15 = filterDefrelPrime v_15 (fromto_D2 1 v_15)
  eulerLL_0 v_15 = (fix eulerLL_0 v_164) (length v_164));

eulerLL_1 v_16 v_17 = case v_17
of {
  <0> v_168 v_169 ->
  seq (v_168 v_169) Pack{0,0};
  <1> -> Pack{0,0}
};

eulerLL_0 v_18 = eulerLL_1 v_18;

ifte v_19 v_20 v_21 = case v_19
of {
  <1> -> v_20;
  <0> -> v_21
};

length v_22 = case v_22 of {
  <1> -> 0;
  <0> v_170 v_171 -> let
  v_171 = length v_171
  in
  (par (lengthLL_0 v_174) (lengthLL_0 v_174));
};

lengthLL_0 v_23
= seq v_23 Pack{0,0};

filterDefrelPrime v_24 v_25
= case v_25 of {
  <1> -> Pack{1,0};
  <0> v_175 v_176 -> let
  v_183 = relPrime v_24 v_175
  in
  (par (filterDefrelPrimeLL_0 v_183)
  (ifte v_183 (Pack{0,2} v_175)
  (filterDefrelPrime
  v_24 v_176))
  (filterDefrelPrime v_24 v_176)));
};
```

number of reductions
on the main thread

Empirical Investigation

RQs: speed-up

```
euler v_15 = let
  v_164 = filterDefrelPrime v_15 (fromto_D2 1 v_15)
  in (fix eulerLL_0 v_164) (length v_164);

eulerLL_1 v_16 v_17 = case v_17
of {
  <0> v_168 v_169 ->
  seq (v_168 v_169) Pack{0,0};
  <1> -> Pack{0,0}
};

eulerLL_0 v_18 = eulerLL_1 v_18;

ifte v_19 v_20 v_21 = case v_19
of {
  <1> -> v_20;
  <0> -> v_21
};

length v_22 = case v_22 of {
  <1> -> 0;
  <0> v_170 v_171 -> let
    v_174 = length v_171
  in (par (lengthLL_0 v_174) (1 + v_174))
};

lengthLL_0 v_23
= seq v_23 Pack{0,0};

filterDefrelPrime v_24 v_25
= case v_25 of {
  <1> -> Pack{1,0};
  <0> v_175 v_176 -> let
    v_183 = relPrime v_24 v_175
  in
  (par (filterDefrelPrimeLL_0 v_183)
    (ifte v_183 (Pack{0,2} v_175) (filterDefrelPrime
      v_24 v_176)))
};
```

all pars

```
euler v_15 = let
  v_164 = filterDefrelPrime v_15 (fromto_D2 1 v_15)
  in (fix eulerLL_0 v_164) (length v_164);

eulerLL_1 v_16 v_17 = case v_17
of {
  <0> v_168 v_169 ->
  seq (v_168 v_169) Pack{0,0};
  <1> -> Pack{0,0}
};

eulerLL_0 v_18 = eulerLL_1 v_18;

ifte v_19 v_20 v_21 = case v_19
of {
  <1> -> v_20;
  <0> -> v_21
};

length v_22 = case v_22 of {
  <1> -> 0;
  <0> v_170 v_171 -> let
    v_174 = length v_171
  in
  (par (lengthLL_0 v_174) (1 + v_174))
};

lengthLL_0 v_23
= seq v_23 Pack{0,0};

filterDefrelPrime v_24 v_25
= case v_25 of {
  <1> -> Pack{1,0};
  <0> v_175 v_176 -> let
    v_183 = relPrime v_24 v_175
  in
  (par (filterDefrelPrimeLL_0 v_183)
    (ifte v_183 (Pack{0,2} v_175) (filterDefrelPrime
      v_24 v_176)))
};
```

optimised pars

```
euler v_15 = let
  v_164 = filterDefrelPrime v_15 (fromto_D2 1 v_15)
  in
  (par (fix eulerLL_0 v_164) (length v_164));

eulerLL_1 v_16 v_17 = case v_17
of {
  <0> v_168 v_169 ->
  seq (v_168 v_169) Pack{0,0};
  <1> -> Pack{0,0}
};

eulerLL_0 v_18 = eulerLL_1 v_18;

ifte v_19 v_20 v_21 = case v_19
of {
  <1> -> v_20;
  <0> -> v_21
};

length v_22 = case v_22 of {
  <1> -> 0;
  <0> v_170 v_171 -> let
    v_174 = length v_171
  in
  (par (lengthLL_0 v_174) ((1 + v_174)))
};

lengthLL_0 v_23
= seq v_23 Pack{0,0};

filterDefrelPrime v_24 v_25
= case v_25 of {
  <1> -> Pack{1,0};
  <0> v_175 v_176 -> let
    v_183 = relPrime v_24 v_175
  in
  (par (filterDefrelPrimeLL_0 v_183)
    (ifte v_183 (Pack{0,2} v_175) (filterDefrelPrime
      v_24 v_176)))
};
```

sequential

RQs: search

method

randomised
greedy



simple
hill-climbing

initialisation

all par-sites
enabled



random par-sites
enabled

Programs

SumEuler

Queens

Queens2

SodaCount

Tak

Taut

MatMul

Empirical Method

7 programs

X

2 search methods

X

all par-sites

2 initialisation methods

no par-sites

X

30 repetitions

X

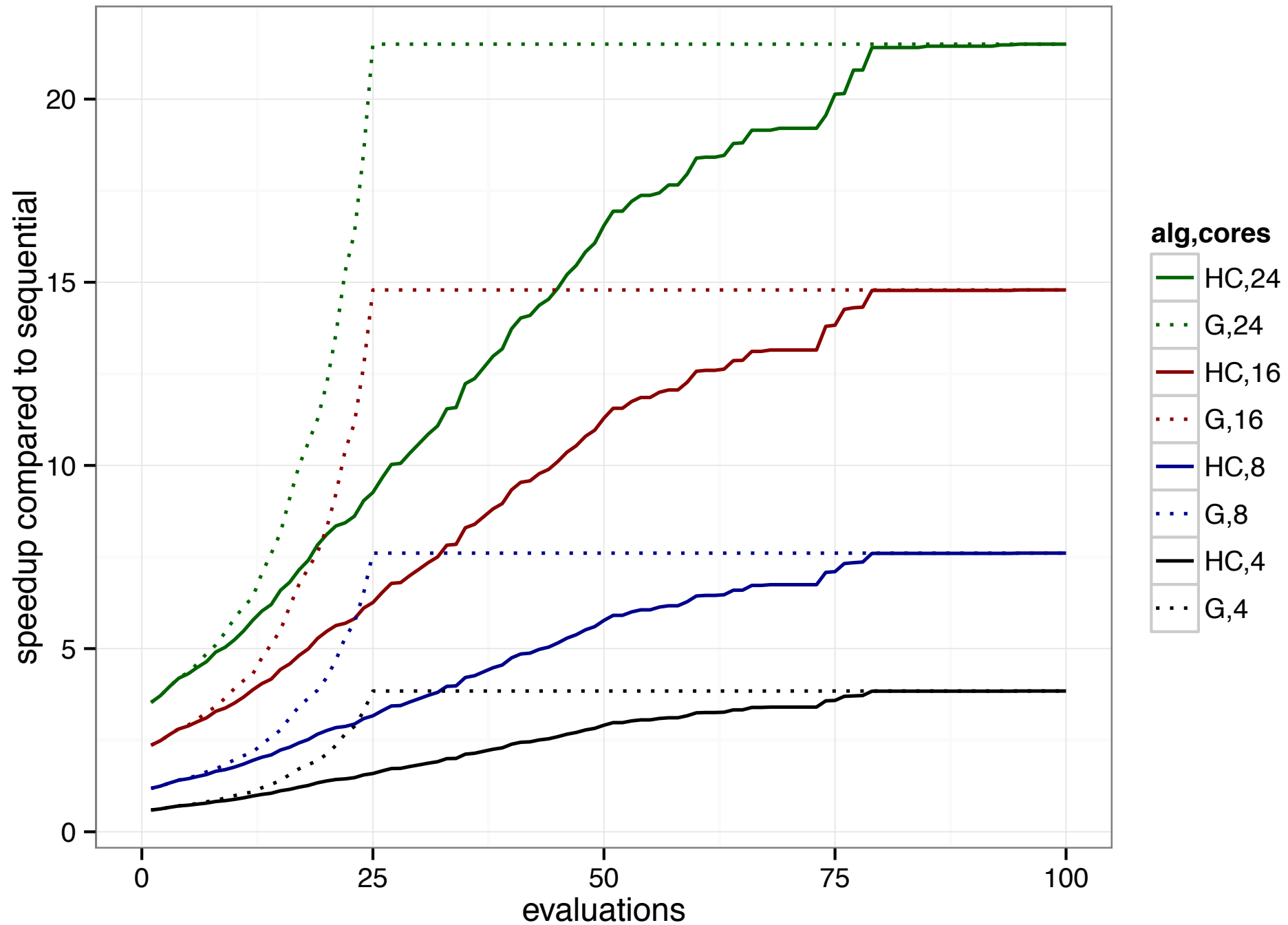
4 target environments (4, 8, 16, 24 cores)

Results: initialisation

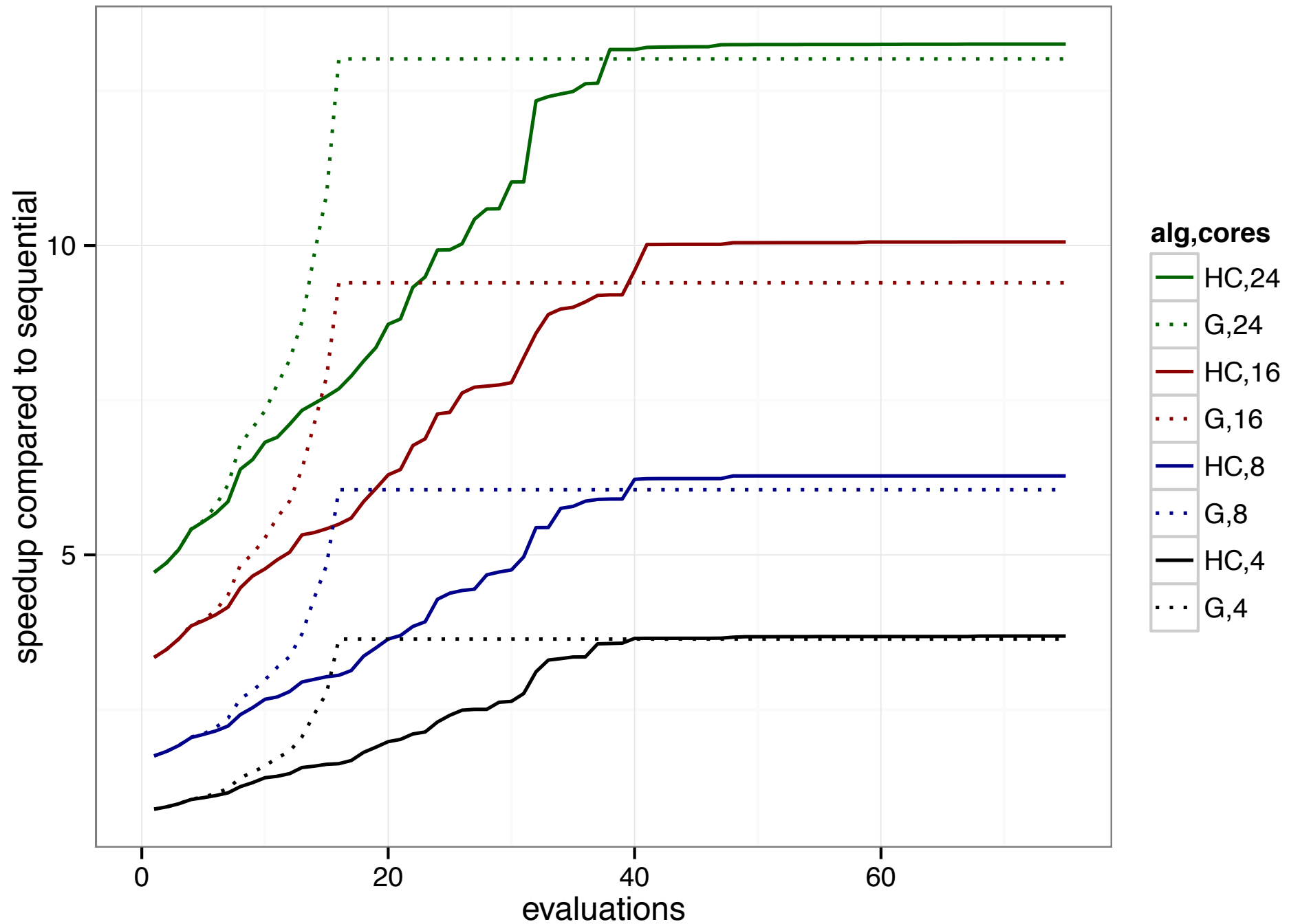
most programs: no significant difference

SodaCount: enabling all `par`-sites was slightly better

Results: Queens2



Results: SodaCount



Conclusions and Future Work

Summary

A combination of static analysis and search that can **automatically** and **effectively** parallelise functional programs to take advantage of parallel computing environments

Future Work

investigate scalability

apply more sophisticated search algorithms